

## AN APPROACH TO NONLINEAR BEHAVIOUR PREDICTION OF TECHNICAL SYSTEMS

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### 1. Introduction

The number of challenges faced by firms in recent years has increased dramatically. Such challenges mainly arise from continued changes in market situations as a result of globalization, quickly reflecting both in international competition, shorter product lifecycles, and technological progress [Simpson et al. 2006]. In addition, customer requirements have been increasingly high, including customized product variants, which firms are to satisfy with their product ranges. To maintain competitiveness, firms should not ignore such requirements [Anggraeni et al. 2013]. Such increased number of product variants implies a greater complexity of the product development processes [Robertson and Ulrich 1998]. One may argue that the crucial factor of an industrial company's performance arises from its ability to comprehend and operate complex systems, as well as their development processes, and constant adoption of new technologies. Knowledge so acquired should be used as a competitive advantage in product development and improvement. However, this is becoming increasingly difficult nowadays, as a result of a drastic increase in system (product) complexity [Diepold et al. 2010]. So it is therefore necessary to be able to describe the system architecture and to model its behaviour to better understand the system itself [Diepold et al. 2010a]. When creating new or improving existing product variants by changing the system architecture or adding functions or subsystems, we are able to influence its behaviour. However, it is very difficult to identify "good" product architectures [Wyatt et al. 2011].

Designing may be described as a process of transforming a set of needs and requirements into a technical system description [Hubka and Eder 1992], [Hubka and Eder 1988]. In an area determined by user requirements, the designer iteratively advances from an abstract idea and concept to a specifically designed and detailed solution. Its iteration is characterized by a series of loops with alternating solution generation and validation, based on which the designer makes decisions on certain future solutions. The designing process begins with imprecise, incomplete and often contradictory information about the future product and each alternative to the solution is designed as a transformation of a set of criteria and/or requirements into a theoretical or physical solution, including designer's experience. Decisions made during the preliminary phases of product development have a substantial impact on the product (e.g. product development time in relation to product quality and price). Making such decisions is impeded by uncertainty and vagueness, imminent to initial phases of product development [Stark et al. 2010]. As a result of technological progress and adaptations in use, technical systems may be found in a working environment not included in the initial specification, which results in uncertain working conditions (e.g. operation of an environmental chamber at low external temperatures or operation of a load lifting device as a result of high wind speeds). In addition, the initial phases of product development include many uncertain parameters, which should be considered as such when evaluating product alternatives and making decisions [Kota and Chakabarti

2009]. Two most influential aspects intertwine in different product development phases, on different levels: creating the system architecture and parallel valuation of proposed architecture's behaviour [Hubka and Eder 1992], [Hansen and Andreassen 2002].

This paper represents an approach to the architecture development for complex technical systems based on their nonlinear behaviour model. It provides us with feedback on the behaviour of proposed system architectures (more precisely, their subsystems) in two cases. One case is under specified working conditions, while the other one is under uncertain conditions during system operation. In this case, uncertain conditions are those resulting from external influences (natural uncertainty [Kota and Chakabarti 2009]). In addition, this approach allows us to model and simulate the behaviour of a complex nonlinear technical system and test its stability. System modelling by using our mathematical model allows us to take into account the uncertainties resulting from external conditions (e.g. the impact of external temperature, air pressure or high-speed winds affecting the system). In addition to all this, it allows us to record the behaviour of the observed system by using fuzzy rules. The approach has an iterative character, which means it is possible to affect the behaviour of a technical system by adding or removing certain subsystems in its architecture (by changing it). Recording behaviour rules allows us to improve the present system by adding new behaviour rules.

The next section describes the background and addresses the previous research in connection with the development and validation of system architecture, including uncertain working conditions. This paper is an extension of such research. Section 3 motivated us to continue this research, while Chapter 4 provides a brief description of the approach, explained on a step-by-step basis, and transfer of information between steps. Section 5 provides a verification of the approach on an example of a load lifting device. A discussion of the results obtained on such example is provided in Section 6. Section 7, which closes this paper, provides a conclusion of the presented research and possible directions of future research.

## **2. Background**

Two main approaches known in recent years, which is applies in the development and validation of alternatives of technical system architectures. One approach is based on Robust Design and methods developed mostly by [Taguchi 1993], where existing models and product development methods are integrated. The other approach, so-called Multi-Dynamic Mapping [Diepold et al. 2010], [Diepold et al. 2010] integrates structural and dynamical complexity according to Strogatz [2001], with bilateral information mapping between the structural domain and the behavioral domain. Both approaches have advantages and flaws that are often manifested in a number of ways, depending on the system domain. Some of the second approach's flaws were attempted to be resolved by research in the Osman et al [2011] paper, directing the the research to the application of the Behaviour Prediction Framework in the development of complex technical systems. BPF approach is based on the Multi-Dynamic Mapping, where it provides bilateral information mapping by combining the structural model and the behavioral model (dynamic models) of the technical system. It also eliminates certain flaws of Multi-Dynamic Mapping such as: the possibility of mathematical subsystem behaviour modeling depending on time, so-called non-stationary model, the possibility of presenting the system in a nonlinear form, and the possibility of improving the system within the dynamic model by changing the parameters. This reduces the potential number of iteration steps while seeking a satisfactory solution. The approach is also applicable to large systems. The approach was tested on an environmental chamber technical system as an example of a highly linear system with substantial delays.

## **3. Motivation**

The product validation and decision making process is particularly important in the conceptual phase of product development. It is in this phase that we are able to avoid potential designing errors and eliminate them before they spread to later development phases. In product development, it is particularly important to resolve problems relating to uncertainty resulting from natural impacts (so-called natural uncertainty) [Kota and Chakabarti 2009]. Such problems are very difficult to resolve without having knowledge of technical system behaviour and the possibilities of their mathematical modeling. This depends on the technical system's type and application. Where such situations arise,

standard approaches provide unsatisfactory results because they fail to provide a quantitative comparison between product variants and therefore fail to determine the acceptable situation. In addition, current product validation processes are becoming increasingly complex. There are multiple reasons for this, of which we will underscore two according to [Kortler et al. 2012]: primarily, increasingly complex customer requirements and enhanced technical possibilities of the equipment manufacturer. In addition, multidisciplinary and integration of several professions (mechanical engineering, electronics, computing, maintenance) in the development of modern products (such as mechatronic systems) increases the complexity of the validation process [Lindemann 2006]. This paper aims to present an approach based on the development of technical system architectures according to their behaviour models. Irrespective of the domain of application, the most important flaw in the approaches referred to in Section 2 of this paper is that neither approach supports a non-stationary presentation of technical system architecture behaviour. Based on the system's mathematical model, prediction of its behaviour, and an assessment of the simulation and system stability testing quality, we attempted to create a decision making model based on Mamdani-type decision making and recording behaviour by using fuzzy rules. We aimed to apply this to a group of technical systems according to their behaviour, so-called highly nonlinear systems. A nonlinear mathematical model can be linearized (approximated by using a linear model) depending on the designated operating mode. This will result in a linear mathematical model where it will be possible to explain system behaviour in a satisfactory manner in a framework of a selected state of balance (because linear effects of the system prevail). This paper also contemplates dynamic system models with concentrated parameters.

#### 4. Proposed approach

The proposed approach to the development of nonlinear technical system architectures is presented in Figure 1, and consists of 6 basic steps. They are listed below, including their brief descriptions:

1. Description of the proposed system architecture – by using the DSM (Design Structure Matrix) [Steward 1981], [Lindemann et al. 2009]. The initial step within this approach, repeated after each new iteration step, is to add or remove particular subsystems, after which new subsystems are analyzed using a bulking process according to the DSM. The present computing tool *LOOME*® is used.
2. Creation of the system behaviour mathematical model [Close et al. 2002] – based on the subsystems obtained in the preceding step, but subject to the requirements and simplifications introduced, mathematical behavioral models are created for both domains (continuous and discrete), recorded in a space state form [Williams and Lawrence 2007]. Such mathematical behavioral models are recorded as *m* files within the present computing tool *MATLAB*®.
3. Simulation of the system behaviour by using the Model Predictive Control (MPC) method [Camacho and Bordons 2004], [Mayne et al. 2000] – based on the mathematical models created in the preceding step (by using the mathematical behavioral model in a state space) and by adjusting certain parameters according to the MPC method, we aim to provide a better technical system behaviour simulation. System behaviour is simulated by using the present computing tool *MATLAB Model Predictive Control Toolbox*®.
4. Test of system stability – the simulated technical system is tested in its behavioral domain by using Lyapunov's direct method [Vukić and Kuljača 2005]. The procedure for testing system stability was created within the present computing tool *MATLAB*®.
5. Decision making – creation of the fuzzy behavioral rules based on the influential parameters provided by the mathematical model and the knowledge gained about system behaviour (through steps 3 and 4 of the described approach). The decision making system's output may be observed graphically, on a local or global decision making level. The Fuzzy Rule Based System and Mamdani decision making model [Mamdani 1982] are used for this purpose. The *MATLAB Fuzzy Control System Toolbox*® is used, which supports the record of the Mamdani fuzzy behavioral model [Mamdani 1975]. Note: the influential parameters are determined by the designer based on experience.



- **Steps 4 – 5** – the information about system stability (unstable, asymptotically stable or globally stable) is later used as an output variable when creating fuzzy behavioral rules.
- **Steps 5 – 6** – a system (process) found to have a satisfactory behaviour in the preceding steps (a stable system for most input variables) and to be stable under uncertain operating conditions may be proposed for a newly developed variant of an existing technical system. In case the system's behaviour is not satisfactory and the system is unstable under uncertain operating conditions, the entire procedure is repeated, starting from step 1. By altering customer or engineering requirements, new subsystems are added or existing ones are removed in the overall technical system. Such approach is referred to as iterative because it takes several iteration steps to come to a satisfactory solution.

## 5. Case study – load lifting device

An electric motor system, (load lifting device) used for lifting loads in shipyards as part of a crane was selected as an example of a complex technical system with nonlinear behaviour. Generally, the system consists of the following subsystems: an electric motor-driven power transmission and a load lifting drum with steel rope and a hook. During its operation, the device was exposed to atmospheric impacts and was tested in variable operating conditions, particularly in uncertain operating conditions where strong gusts of wind are present.

The initial architecture of the lifting device is created on the basis of the customer requirements received and the resulting engineering requirements. The lifting device's system consists of the following subsystems: a three-phase asynchronous electric motor, a drive and a output shaft, clutches on the drive and output shafts, bearings, a single-speed power transmission, a lifting grooved drum, wire rope and a load securing hook (presented in Figure 2a).

**The customer requirements** are as follows:

- the device must be suitable for exterior installation,
- the device must be able to operate in variable external operation conditions,
- the device must be resistant to atmospheric impacts (water, rain, snow, ice, air, gusts of wind),
- the device is intended to be installed on cranes in shipyards,
- the device must have an automated control option.

**The engineering requirements** are as follows:

- the device is situated within the coastal belt (Croatia – EU member state),
- the device must be able to operate at high wind speeds: up to 100 km/h (Zone 3),
- the device must be provided with uninterrupted electricity supply, 3x220 V, 50 Hz,
- the device must be provided with an interrupted operating mode,
- the device must be capable of lifting and lowering loads,
- the electric motor driving the device must be able to operate at variable rotational speeds,
- the device is intended for lifting smaller loads of up to 10 t,
- loads should be lifted and lowered by using the hook,
- the device must be resistant to shock and vibration,
- operating stability of the device must be ensured.

According to the steps of the approach described (in the preceding section), the DSM first used to describe the proposed system architecture and an analysis resulted in possible subsystems.

### Step 1

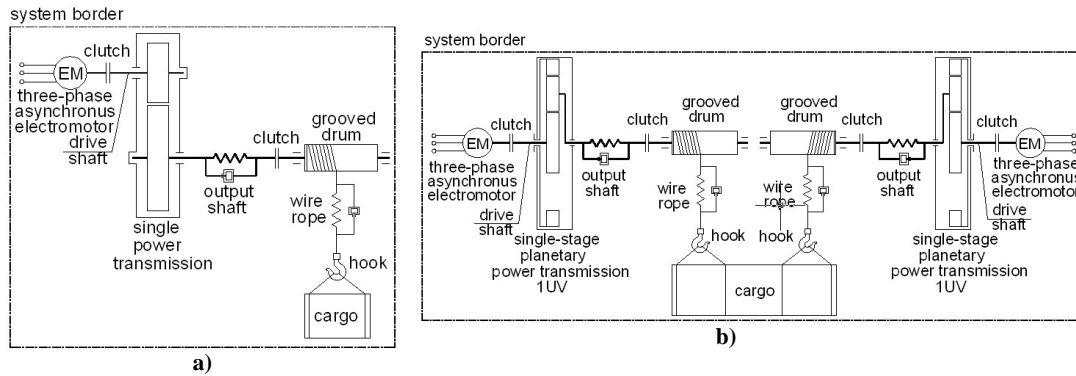
The results obtained by using the DSM [Steward 1981], [Lindemann et al. 2009] are presented in Figure 3a. According to the subsystems given by DSM and the initial assumptions, we proceeded to create a mathematical model for the system.

### Step 2

*The initial assumptions* that we applied to the modeling of a mathematical behavioral model for the respective subsystems of the lifting device are as follows:

- all losses in bearings, gears and clutches are neglected,
- all resistance resulting from driving the device on a railway are neglected,
- all losses in the lifting mechanism occurring during operation and standby are neglected,
- the resistance taken into consideration is the resistance resulting from the effect of wind,

- because of the assumption that is the compact design of the three-phase asynchronous motor and power transmission with a clutch, the driving shaft is assumed to be designed as an ideal solid body,
- the driven shaft and steel rope are assumed to be designed as an elastic body,
- the load is assumed to be of a rectangular shape and its volume is  $V=abc$  [m<sup>3</sup>],
- loads are assumed to be directly lifted/lowered by using the drum and the steel hook,
- the device's assumed drivetrain is drivetrain 2 [DIN 15018 1984],
- the weight of the rope in relation to the weight of the hook and load is neglected because the ratio is  $\frac{m_K+m_T}{m_u} \cong 20 \div 200$ ,
- low vibrations are assumed in the system [Bazjanac 1974],
- the viscous damping coefficient  $k_u$  of the steel rope is very small and may be neglected [Feyver 2007].



**Figure 2. Load lifting device system architecture: a) initial system architecture - iteration 1, b) final system architecture – iteration 4**

Resistance resulting from wind gusts is considered as a possibility in unexpected operating conditions. As the device is assumed to be installed on a crane within the coastal zone of the Republic of Croatia, the relevant wind speed zone is zone 3 [ISO 4302 1981]. According to the steps of the approach described (in the preceding section), the DSM first used to create the system architecture and possible subsystems were identified. The results obtained by using the DSM are presented in Figure 3a. The mathematical model creates differential equations of mechanism's motion by using Lagrange's equations of the second type for mechanical systems in the most general form (with  $s$  degrees of freedom of motion) [Bazjanac 1974].

After all assumptions, linearization and neglects in the mathematical model, the final form of the technical system motion differential equations is:

$$\varphi_0 = \frac{1}{J_0 + J_1 + J_2 \cdot \frac{1}{i^2}} [c_{GV} \varphi_5 - \frac{1}{i^2} \varphi_0 + k_{GV} \varphi_5 - \frac{1}{i} \varphi_0 \frac{1}{i} - M_{EM}] \quad (1),$$

$$\varphi_5 = - \frac{1}{1 + m_{uk} r_B^2 \frac{1}{1+g} J_5 + m_{uk} r_B^2} [m_{uk} r_B (r_B (1 + g) \varphi_5 + l_1 \varphi_6) + r_B F_V \varphi_6 - c_{GV} \varphi_5 - \frac{1}{i^2} \varphi_0 - \frac{A_u E_u r_B}{2} r_B \varphi_5 - k_{GV} \varphi_5 - \frac{1}{i} \varphi_0] \quad (2),$$

$$\varphi_6 = - \frac{1}{2 l_1^2} [m_{uk} g l_1 \varphi_6 - F_V r_B \varphi_5] \quad (3).$$

Based on the given equations ((1) – (3)), a record of the load lifting device mathematical behavioral model is created in the state space [Williams and Lawrence 2007]. Also based on the given variables and matrices in state space form, a model record and the source code is created in the existing *MATLAB*® software.

### Step 3

When simulating behaviour and testing system stability, influential variables presented in Table 1 are used (in all iterations).

**Legend** (for variables in equations (1) – (3)):

$c_{GV}$  [N/m] – torsional stiffness of output shaft

$F_V$  [N] – wind force

$g$  [m/s<sup>2</sup>] – gravitational constant;  $g = 9.81$  m/s<sup>2</sup>

$i$  [-] – total transmission ratio

$J_0$  [kgm<sup>2</sup>] – dynamic moment of inertia of electromotor

$J_1$  [kgm<sup>2</sup>] – dynamic moment of inertia of gear 1

$J_2$  [kgm<sup>2</sup>] – dynamic moment of inertia of gear 2

$J_5$  [kgm<sup>2</sup>] – dynamic moment of inertia of grooved drum

$k_{GV}$  [Ns/m] – viscous damping coefficient of output shaft

$l_1$  [m] – initial wire rope length

$M_{EM}$  [Nm] – moment of electromotor

$m_{uk}$  [kg] – total mass

$r_B$  [m] – grooved drum radius

$\varphi_0$  [rad] – twist angle of electromotor

$\varphi_5$  [rad] – twist angle of grooved drum

$\varphi_6$  [rad] – twist angle of wire rope

$\dot{\varphi}_0$  [rad/s] – angular velocity of electromotor

$\dot{\varphi}_5$  [rad/s] – angular velocity of grooved drum

$\ddot{\varphi}_0$  [rad/s<sup>2</sup>] – angular acceleration of electromotor

$\ddot{\varphi}_5$  [rad/s<sup>2</sup>] – angular acceleration of grooved drum

$\ddot{\varphi}_6$  [rad/s<sup>2</sup>] – angular acceleration of wire rope

As shown, the influential variables (selected by the designer based on his experience) are:  $n_M$  [min<sup>-1</sup>] – electromotor rotational speed (a),  $i$  [-] – total transmission ratio in the power transmission (b),  $m_T$  [t] – load weight (c),  $v_V$  [t] – wind velocity (d), and weight factor  $\rho$  [-] (e).

**Table 1. Presentation of the range of influential variables (in iterations 1 - 4)**

iteration	1 – 2	3	4
$n_M$ [min <sup>-1</sup> ]	600 – 3000	600 – 3000	600 – 3000
$i$ [-]	10 – 200	200 – 400	200 – 400
$m_T$ [t]	1 – 10	1 – 10	10 – 20
$v_V$ [km/h]	50 – 100	50 – 100	50 – 100
$\rho$ [-]	0 – 1	0 – 1	0 – 1

The variables mutually vary during the testing of the technical system's behaviour (simulation of its behaviour [Camacho and Bordons 2004], [Mayne et al. 2000] and testing of system stability [Vukić and Kuljača 2005]) in all iterations.

### Step 4 and Step 5

Based on such results, fuzzy behavioral rules are created by using the decision making system [Mamdani 1982]. The behavioral rules are based on Mamdani's fuzzy logic model [Mamdani 1975]. The decision making system in the existing *MATLAB Fuzzy Logic Toolbox*® software is used for that purpose. The semantics of the influential variables used to create fuzzy rules in iterations 1 and 2 are presented in Table 2. The responses obtained by using the MPC method and Lyapunov's stability testing method are presented in Figures 3b and 3c. The results obtained by global inference (for the input variables  $n_M$  and  $v_V$ ) are presented in Figure 3d. The obtained results will be further commented in Section 6 of this paper.

### Step 6

Another speed will be added to the power transmission in next iteration to allow for an increase in the transmission ratio and obtain a more stable system at higher wind speeds. In the third iteration, a simple planetary transmission was used 1UV [Opalić 1998], to allow for the device to operate with

higher transmission ratios and to increase the load lifting/lowering speed. The system behaviour mathematical model in iteration steps was changed insignificantly. In iteration 4 was demonstrated that this approach allowed for new behavioral rules to be introduced with satisfactory test results. Another system was added, having identical subsystems as that in iteration 3. This was intended to allow for concurrent lifting and lowering of large loads. Based on experience, two load-lifting devices, each with its drive, provide more stable operation when lifting heavy loads from greater heights, at higher lifting speeds.

**Table 2. Presentation of the semantics of influential variables to create fuzzy rules (in iteration 1 and 2)**

a)

$n_M [\text{min}^{-1}]$	Span	Semantics
600 – 1000	0	Very small
1000 – 1500	0.25	Small
1500 – 2000	0.5	Medium
2000 – 2500	0.75	High
2500 – 3000	1	Very high

b)

$i [-]$	Span	Semantics
10 – 40	0	Very small
40 – 80	0.25	Small
80 – 120	0.5	Medium
120–160	0.75	High
160 – 200	1	Very high

c)

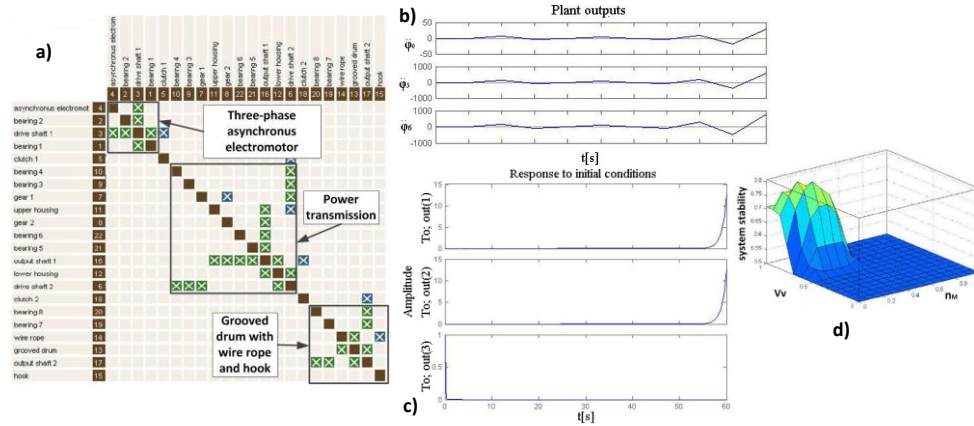
$m_T [\text{t}]$	Span	Semantics
1 – 2	0	Very small
2 – 4	0.25	Small
4 – 6	0.5	Medium
6 – 8	0.75	High
8 – 10	1	Very high

d)

$v_T [\text{t}]$	Span	Semantics
50 – 60	0	Very small
60 – 70	0.25	Small
70 – 80	0.5	Medium
80 – 90	0.75	High
90 – 100	1	Very high

e)

$\rho [-]$	Span	Semantics
0 – 0.2	0	Very small
0.2 – 0.4	0.25	Small
0.4 – 0.6	0.5	Medium
0.6 – 0.8	0.75	High
0.8 – 1	1	Very high



**Figure 3. Obtained results for the initial architecture of the load lifting device (iteration 1); a) DSM, b) MPC method – output variable responses, c) stability testing by using Lyapunov's direct method, and d) global inference results for the input variables  $n_M$  and  $v_V$**

The same differential equations as those in iteration 1 apply, provided that iteration 2 also takes into account the two-speed transmission in the mechanism motion equation (which is also taken into account in iteration 3). Iteration 4 is takes into account all equations in iteration 3 and 4, plus envisaging that a load lifting device only picks up half the load weight  $m_T/2$ . The semantics of the influential variables used to create fuzzy rules in iteration 3 and 4 is presented in Table 3.

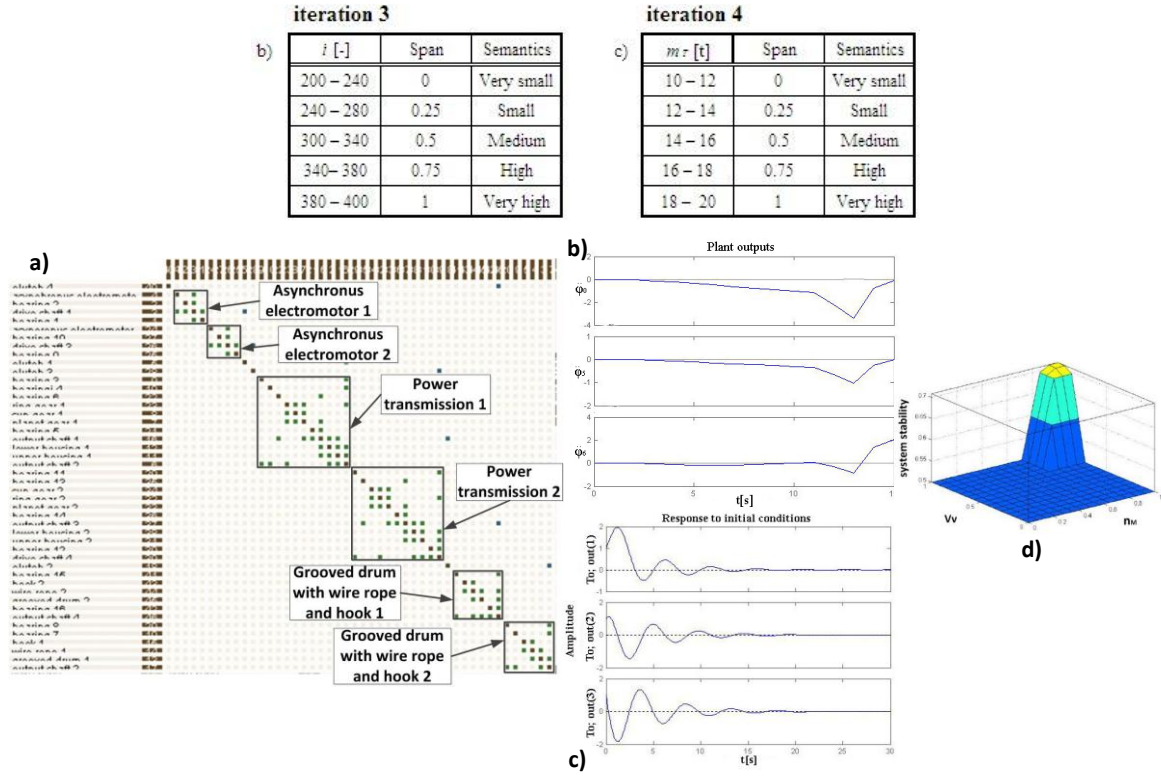
For iteration 3 only the semantics for the variable transmission ratio  $i$  variable are presented, which variable changes in relation to the preceding two iteration steps. Also for the iteration 4 only the semantics for the variable load weight  $m_T$  variable are presented, which variable changes in relation to the preceding iterations. Figure 2b are presented final system architecture after adding new behavioral rules.

The responses obtained by using the MPC method and Lyapunov's stability testing method in iteration 4 are presented in Figures 4b and 4c.

The results obtained by global inference (for the input variables  $n_M$  and  $v_V$ ) are presented in Figure 4d. The obtained results will be further commented in Section 6 of this paper.



**Table 3. Presentation of the semantics of changed influential variables to create fuzzy rules (in iteration 3 and 4)**



**Figure 4. Obtained results for the final architecture of the load lifting device after adding new behaviour rules (iteration 4); a) DSM, b) MPC method – output variable responses, c) stability testing by using Lyapunov's direct method, and d) global inference results for the input variables  $n_M$  and  $v_V$**

## 6. Discussion on obtained results

The approach tested on an example of a complex technical system (a load lifting device) was verified in operation conditions, as well as at high wind speeds and in uncertain operation conditions. Table 4 provides a tabular presentation of the results at the end of each iteration (1 – 4) for each step of the approach (described in the previous section).

In such conditions, the technical system's architecture was developed and its behaviour is tested (the quality of system operation simulation and system stability). The relevant technical system behaviour is of a highly nonlinear nature and was linearized by using a tangential linearization, after additional assumptions have been implemented, and observed as such during the presented research.

On completion of the test (inspection of fuzzy rules and results of local and global inference in each iteration step), we reached several conclusions (provided below):

- high wind velocity  $v_V$  has the greatest impact on system stability at small rotational speeds of the electric motor, ranging between 80 and 100 km/h,
- small rotational speeds of the electric motor in case of large transmission ratios in the power transmission is another great impact on system stability.

In iteration 2, we added new components to the power transmission system and thus reduced the transmission ratio for each transmission speed. The test was conducted by using a two-speed transmission, while iteration 3 used a different type of transmission (planetary transmission). This once again resulted in a system that will be able to operate with large transmission ratios. In iteration 4 was demonstrated that this approach allowed for new behavioral rules to be introduced with satisfactory test results. Another system was added, having identical subsystems as that in iteration 3. This was intended to allow for concurrent lifting and lowering of large loads.

**Table 4. Presentation of the obtained results in each step of the approach after all iterations (1-4)**

Iteration	Approach step	Description
1	System architecture	Subsystems: three-phase asynchronous electric motor, single-speed power transmission with a drive and a output shaft, clutches on the drive and output shafts and bearings, lifting grooved drum with wire rope, and load hook
	System behaviour mathematical model	A system of standard linear differential equations obtained after the linearization procedure (presented in the state space form)
	MPC method	Effective system management can be achieved, except in the unstable area
	System stability testing	The system displays unstable behaviour in case of low and very high electric motor rotational speeds, with high transmission ratios, load weights and wind velocities
2	System architecture	Subsystems: three-phase asynchronous electric motor, two-speed power transmission with a drive and a output shaft, clutches on the drive and output shafts and bearings, lifting grooved drum with wire rope, and load hook
	System behaviour mathematical model	A system of standard linear differential equations obtained after the linearization procedure (presented in the state space)
	MPC method	Effective system management can be achieved, except in the unstable area
	System stability testing	The system displays unstable behaviour in case of low and very high electric motor rotational speeds, with high transmission ratios, load weights and wind velocities
3	System architecture	Subsystems: three-phase asynchronous electric motor, simple planetary transmission with a drive and a output shaft, clutches on the drive and output shafts and bearings, lifting grooved drum with wire rope, and load hook
	System behaviour mathematical model	A system of standard linear differential equations obtained after the linearization procedure (presented in the state space)
	MPC method	Effective system management can be achieved, except in the unstable area
	System stability testing	The system displays unstable behaviour in case of low and very high electric motor rotational speeds, with high transmission ratios, load weights and wind velocities
4	System architecture	Same two systems with the following subsystems: three-phase asynchronous electric motor, single-stage planetary transmission with a drive and a output shaft, clutches on the drive and output shafts and bearings, lifting grooved drum with wire rope, and load hook
	System behaviour mathematical model	A system of standard linear differential equations obtained after the linearization procedure (presented in the state space)
	MPC method	Effective system management can be achieved, except in the unstable area
	System stability testing	The system displays unstable behaviour in case of low and very high electric motor rotational speeds, with high transmission ratios, load weights and wind velocities

Both systems operate in a synchronized manner (at the same electric motor speeds and the same load lifting and lowering speeds). By changing the power transmission subsystem through several iteration steps, we demonstrated that the device was able to operate in uncertain operating conditions, at high wind speeds. The following may be concluded on the basis of the global inference, where the electromotor rotational speed  $n_M$  and wind velocity  $v_V$  were put in a correlation as input variables, if system stability is treated as the result. By adding new behaviour rules, we managed to achieve stable operation of the system for low rotational speeds of the electromotor and medium to high velocities of wind, the force of which burdens the load.

## 7. Conclusion and future research

The objective of the research presented in this paper is to develop an approach modeling and predicting the nonlinear behaviour of complex technical systems in the operating environment, based on a presentation of the system's dynamic behaviour and recording of such behaviour by using the rules. This approach should help develop new structures of nonlinear complex systems and improve existing ones, by mapping in both directions, from the structural to the behavioral domain and vice versa. It should be mentioned that the research completed was not intended to develop new modeling methods, but to provide a new approach to describing the architecture of complex technical systems. If the existing modeling methods are used, the approach will also allow us to predict behaviour in the operating environment.

This paper also presents a verification of the approach on an example of a highly nonlinear behaviour of technical system (example: load lifting device). It was demonstrated through several iterations in the verification that the use of the system with new subsystems added may cause the behaviour of such systems to change during the development of their respective architectures. The approach also allows us to include disturbance variables in the mathematical behavioral model, which cause uncertain operating conditions. Predicting behaviour by using the MPC method allows us to develop technical system architectures based on known behaviour of similar technical systems (by using the influential variable change trajectory). It was also verified whether or not the parameters may be adjusted to effectively simulate the system during its operation in both real conditions and under the effect of uncertain operating conditions. The system stability test once again determines whether or not the nonlinear complex technical system including its subsystems operates in a stable operating area.

Only a theoretical analysis of the presented technical system's behaviour was conducted. However, despite the simulation results, the basic condition precedent to validating the proposed approach in a real environment was its testing and performing experiments in real operating conditions. However, as we are currently unable to conduct such an experiment, it was not included in the research contemplated in this paper. This is the main limitation of the presented research. It may be used as a direction in future research.

Some limitations that could also be used as future research directions are specified below. This is primarily the duration of the procedure for simulating behaviour and testing system stability. A certain number of variables need to be varied by putting them in correlations. Such method could be expedited by expanding the decision making system, enabling automated rule creation and introducing a Neuro – Fuzzy Inference System.

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